



### 3. THE GENERAL CASE

Let

$H$	supply of central bank money (also called monetary base, or high-powered money) (\$)
$CU$	currency held by the non-bank public (\$)
$R$	reserves held by commercial banks
$D$	checkable accounts (also called demand deposits) (\$)
$M$	stock of money (\$)
$\theta$	reserve-deposit ratio: the fraction of deposits that banks hold in reserve ( $R/D$ )
$c$	currency-money demand ratio: shows the preferences of the public about how much money to hold in the form of currency, and how much to hold in the form of checkable accounts.

Superscripts  $d$  and  $s$  denote demand and supply, respectively

The two demands for currency and checkable deposits can be written as:

$$CU^d = cM^d \quad (1)$$

$$D^d = (1 - c)M^d. \quad (2)$$

The demand for reserves (by commercial banks) can be written as:

$$R^d = \theta D^d. \quad (3)$$

Substituting from (2) into (3) for  $D^d$  we get:

$$R^d = \theta(1 - c)M^d \quad (4)$$

Total demand for central bank money can be written as:

$$H^d = CU^d + R^d. \quad (5)$$

Substituting from (1) and (4) into (5), we get:

$$H^d = cM^d + \theta(1 - c)M^d = [c + \theta(1 - c)]M^d. \quad (6)$$

In equilibrium, supply of central bank money,  $H$ , is equal to demand,  $H^d$ . That is:

$$H = [c + \theta(1 - c)]M^d.$$

Dividing both sides by the expression in the brackets, we get:

$$\frac{1}{[c + \theta(1 - c)]} H = M^d. \quad (7)$$

So the formula for the money supply is:

$$M^s = \frac{1}{[c + \theta(1 - c)]} H. \quad (8)$$

The expression  $\frac{1}{[c + \theta(1 - c)]}$  is called the *money multiplier*.

Note that in *EXTREME CASE 1*,  $c = 0$ , therefore the money multiplier is  $\frac{1}{\theta}$ . In *EXTREME CASE 2*, however,  $c = 1$ , so the money multiplier in this case is  $= 1$ .

Rough estimates for  $\theta$  and  $c$ , for the U.S., before the financial crisis which led to the Great Recession were, respectively: 0.10 and 0.40. Plugging these values into the money multiplier formula we get:

$$\frac{1}{[0.40 + 0.10(1 - 0.40)]} = 2.17.$$

