

The Phillips Curve, the Natural Rate of Unemployment, and Inflation

1. Background

Revisit the original price-setting equation: $P = P^e (1 + m)F(u, z)$ (1)

Assume the following simple functional form: $F(u, z) = 1 - \alpha u + z$ (2)

Substituting from (2) into (1) we get: $P = P^e (1 + m)(1 - \alpha u + z)$ (3)

After some manipulation (see p. 159 of the textbook) we get:

$$\pi = \pi^e + (m + z) - \alpha u$$
 (4)

Or, equivalently: $\pi_t = \pi_t^e + (m + z) - \alpha u_t$ (5)

2. The Early Phillips Curve

$$\pi_t = (m + z) - \alpha u_t$$
 (6)

3. Expectation Formation

$$\pi_t^e = \theta \pi_{t-1}$$
 (7)

4. The Natural Rate of Unemployment

When $\pi_t = \pi_t^e$, u will be equal to u_n . From (5) above we get:

$$0 = (m + z) - \alpha u_n$$
 (8)

Solving for u_n we get:

$$u_n = \frac{m + z}{\alpha}$$
 (9)

Now, rewrite (5) as:

$$\pi_t - \pi_t^e = -\alpha \left(u_t - \frac{m + z}{\alpha} \right)$$
 (10)

Now, from (9) substitute into (10):

$$\pi_t - \pi_t^e = -\alpha (u_t - u_n)$$
 (11)